

Unsupervised Audio-visual Speech Enhancement based on Variational Autoencoders

Mostafa SADEGHI

* Joint work with Simon LEGLAIVE, Xavier ALAMEDA-PINEDA, Laurent GIRIN, and Radu HORAUD

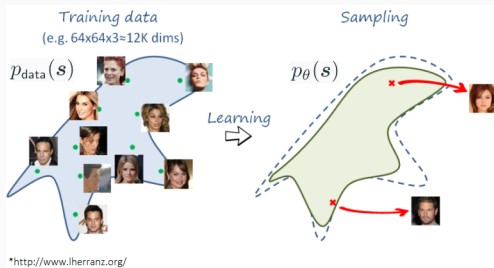
Perception team, Inria Grenoble Rhône-Alpes, France

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- 2 Audio-visual Speech Enhancement
- 3 Robust Audio-visual Speech Enhancement
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Deep Latent Variable Generative Models

Generative Models



Objective: Learning/simulating a complicated probability distribution of data, p_{data} , given some training samples: $s_i \sim p_{\text{data}}(s)$, $i = 1, \dots, N$.

Learn a parametric distribution $p_{\theta}(s)$ as close as possible to $p_{\text{data}}(s)$:

$$\begin{aligned}\theta^* &= \operatorname{argmin}_{\theta} D_{\text{KL}}\left(p_{\text{data}}(s) \parallel p_{\theta}(s)\right) = \operatorname{argmin}_{\theta} \mathbb{E}_{p_{\text{data}}} \left[\log \frac{p_{\text{data}}(s)}{p_{\theta}(s)} \right] \\ &= \operatorname{argmax}_{\theta} \mathbb{E}_{p_{\text{data}}} \left[\log p_{\theta}(s) \right] \approx \boxed{\operatorname{argmax}_{\theta} \frac{1}{N} \sum_{i=1}^N \log p_{\theta}(s_i)}\end{aligned}$$

Latent Variable Generative Models

Latent variable models provide a flexible and hierarchical way to approximate probability distribution of data:

- $\mathbf{s} \in \mathbb{R}^n$: observed variable
- $\mathbf{z} \in \mathbb{R}^\ell$: latent variable, a concise representation of $\mathbf{s}$ ($\ell \ll n$)

$$\begin{cases} \mathbf{z} \sim p_\theta(\mathbf{z}) \\ \mathbf{s}|\mathbf{z} \sim p_\theta(\mathbf{s}|\mathbf{z}) \end{cases} \rightarrow p_\theta(\mathbf{s}) = \int p_\theta(\mathbf{s}, \mathbf{z}) d\mathbf{z} = \int p_\theta(\mathbf{s}|\mathbf{z}) p_\theta(\mathbf{z}) d\mathbf{z}$$

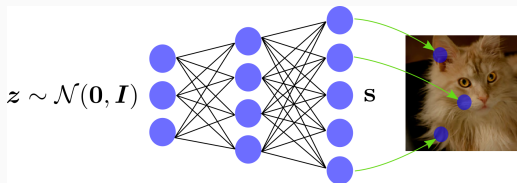
Generating new samples:

Draw $\mathbf{z}_k \sim p_\theta(\mathbf{z})$, then draw a new sample $\mathbf{s}_k \sim p_\theta(\mathbf{s}|\mathbf{z}_k)$

Latent Variable Generative Models

Usually, $p(\mathbf{z}) = \mathcal{N}(\mathbf{0}, \mathbf{I})$, and $p_{\theta}(\mathbf{s}|\mathbf{z})$ is a parametric Gaussian distribution:

- **Linear Gaussian model:** $p_{\theta}(\mathbf{s}|\mathbf{z}) = \mathcal{N}(\mathbf{A}\mathbf{z} + \boldsymbol{\mu}, \sigma^2 \mathbf{I})$
 - $\theta = \{\mathbf{A}, \boldsymbol{\mu}, \sigma\}$
 - Parameter estimation is straightforward
 - Not expressive enough
- **Non-linear Gaussian model:** $p_{\theta}(\mathbf{s}|\mathbf{z}) = \mathcal{N}(\boldsymbol{\mu}_{\theta}(\mathbf{z}), \boldsymbol{\Sigma}_{\theta}(\mathbf{z}))$
 - $\boldsymbol{\mu}_{\theta}(\cdot), \boldsymbol{\Sigma}_{\theta}(\cdot)$: Non-linear functions implemented as deep neural networks
 - Parameter estimation is challenging
 - Often expressive enough



Parameter Estimation

Expectation-Maximization (EM)

$$\begin{aligned}\log p_{\theta}(\mathbf{s}) &= \mathbb{E}_{p_{\theta}(\mathbf{z}|\mathbf{s})} \left[\log p_{\theta}(\mathbf{s}) \right] \\ &= \mathbb{E}_{p_{\theta}(\mathbf{z}|\mathbf{s})} \left[\log \frac{p_{\theta}(\mathbf{s}, \mathbf{z})}{p_{\theta}(\mathbf{z}|\mathbf{s})} \right] \\ &= \mathbb{E}_{p_{\theta}(\mathbf{z}|\mathbf{s})} \left[\log p_{\theta}(\mathbf{s}, \mathbf{z}) \right] - \mathbb{E}_{p_{\theta}(\mathbf{z}|\mathbf{s})} \left[\log p_{\theta}(\mathbf{z}|\mathbf{s}) \right]\end{aligned}$$

- **E-step:** Update the posterior of $\mathbf{z}_i$, $\forall i$:

$$p_{\theta^{old}}(\mathbf{z}_i|\mathbf{s}_i) = \frac{p_{\theta^{old}}(\mathbf{s}_i|\mathbf{z}_i)p(\mathbf{z}_i)}{p_{\theta^{old}}(\mathbf{s}_i)}$$

- **M-step:** Update the parameters:

$$\theta^{new} = \arg \max_{\theta} \frac{1}{N} \sum_{i=1}^N \mathbb{E}_{p_{\theta^{old}}(\mathbf{z}_i|\mathbf{s}_i)} \left[\log p_{\theta}(\mathbf{s}_i, \mathbf{z}_i) \right]$$

Parameter Estimation: Variational Inference

Variational Inference (VI)

- VI seeks an approximate density $q(\mathbf{z}|\mathbf{s})$ by minimizing a measure of dissimilarity:

$$\begin{aligned} D_{\text{KL}}\left(q(\mathbf{z}|\mathbf{s}) \parallel p_{\theta}(\mathbf{z}|\mathbf{s})\right) &= -\mathbb{E}_{q(\mathbf{z}|\mathbf{s})} \left[\log \frac{p_{\theta}(\mathbf{z}|\mathbf{s})}{q(\mathbf{z}|\mathbf{s})} \right] \\ &= -\mathbb{E}_{q(\mathbf{z}|\mathbf{s})} \left[\log \frac{p_{\theta}(\mathbf{s}, \mathbf{z})}{q(\mathbf{z}|\mathbf{s})} \right] + \log p_{\theta}(\mathbf{s}) \geq 0 \end{aligned}$$

- Evidence Lower-bound (ELBO):

$$\text{Evidence} = \log p_{\theta}(\mathbf{s}) \geq \mathbb{E}_{q(\mathbf{z}|\mathbf{s})} \left[\log \frac{p_{\theta}(\mathbf{s}, \mathbf{z})}{q(\mathbf{z}|\mathbf{s})} \right] \triangleq \mathcal{F}(q, \theta)$$

- Optimize the ELBO:

$$q^* = \arg \max_{q \in \mathcal{C}} \mathcal{F}(q, \theta)$$

Parameter Estimation: Variational Inference (continued)

In some cases, the posterior can be computed in closed-form, and $q(z) = p_\theta(z|s)$. As such, the KL term is zero and $\mathcal{F}(q, \theta) = \log p_\theta(s)$.

- **Variational E-step:** For $i = 1, \dots, N$,

$$q_i^{new} = \arg \max_{q_i \in \mathcal{C}} \frac{1}{N} \sum_{j=1}^N \mathcal{F}_j(q_j, \theta^{old})$$

- **M-step:** Update the parameters:

$$\theta^{new} = \arg \max_{\theta} \frac{1}{N} \sum_{j=1}^N \mathcal{F}_j(q_j^{new}, \theta)$$

Parameter Estimation: MCEM

Monte Carlo Expectation-Maximization (MCEM)

- **E-step:** Sample $\{z_i^{(r)}\}_{r=1}^R$ from the posterior of z_i , $\forall i$:

$$p_{\theta^{old}}(z_i | s_i) \propto p_{\theta^{old}}(s_i | z_i) p(z_i)$$

- **M-step:** Update the parameters:

$$\begin{aligned}\theta^{new} &= \arg \max_{\theta} \frac{1}{N} \sum_{i=1}^N \mathbb{E}_{p_{\theta^{old}}(z_i | s_i)} \left[\log p_{\theta}(s_i, z_i) \right] \\ &\approx \arg \max_{\theta} \frac{1}{N} \sum_{i=1}^N \frac{1}{R} \sum_{r=1}^R \log p_{\theta}(s_i, z_i^{(r)})\end{aligned}$$

- Given infinite computational resources, it yields accurate results
- Computationally expensive and not scalable to high-dimensions

Parameter Estimation: Variational Autoencoder

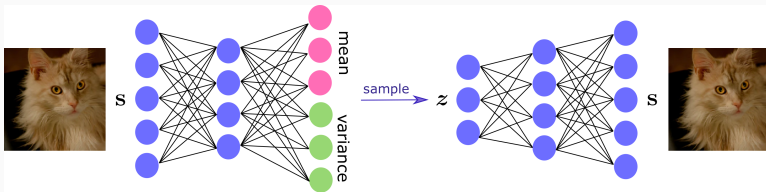
Variational Autoencoder (VAE)

Recall the generative model:
$$\begin{cases} p(z) = \mathcal{N}(\mathbf{0}, \mathbf{I}) \\ p_{\theta}(s|z) = \mathcal{N}(\mu_{\theta}(z), \Sigma_{\theta}(z)) \end{cases}$$

VAE approximates $p_{\theta}(z|s)$ with a *parametric Gaussian distribution*:

$$q_{\psi}(z|s) = \mathcal{N}(\mu_{\psi}(s), \Sigma_{\psi}(s))$$

where, $\mu_{\psi}(\cdot)$ and $\Sigma_{\psi}(\cdot)$ are non-linear functions implemented as *deep neural networks* with parameters ψ . $\Sigma_{\psi}(\cdot)$ is diagonal.



Parameter Estimation: Variational Autoencoder (continued)

The set of parameters $\{\theta, \psi\}$ are estimated by maximizing the ELBO:

$$\begin{aligned}\mathcal{F}(\theta, \psi) &= \mathbb{E}_{q_\psi(\mathbf{z}|\mathbf{s})} \left[\log \frac{p_\theta(\mathbf{s}, \mathbf{z})}{q_\psi(\mathbf{z}|\mathbf{s})} \right] \\ &= \underbrace{\mathbb{E}_{q_\psi(\mathbf{z}|\mathbf{s})} \left[\log p_\theta(\mathbf{s}|\mathbf{z}) \right]}_{\text{Reconstruction term}} - \underbrace{D_{\text{KL}}(q_\psi(\mathbf{z}|\mathbf{s}) \parallel p(\mathbf{z}))}_{\text{Regularization term}} \\ &\approx \log p_\theta(\mathbf{s}|\mathbf{z}_\psi) - D_{\text{KL}}(q_\psi(\mathbf{z}|\mathbf{s}) \parallel p(\mathbf{z}))\end{aligned}$$

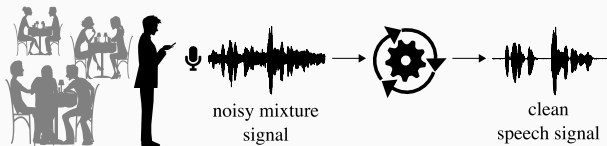
where, $\mathbf{z}_\psi = \boldsymbol{\mu}_\psi(\mathbf{s}) + \boldsymbol{\epsilon} \odot \text{diag}(\boldsymbol{\Sigma}_\psi(\mathbf{s})) \sim q_\psi(\mathbf{z}|\mathbf{s})$, $\boldsymbol{\epsilon} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$

Stochastic gradient descent:

$$\theta^{(new)}, \psi^{(new)} = \arg \max_{\theta, \psi} \frac{1}{N} \sum_{i=1}^N \log p_\theta(\mathbf{s}|\mathbf{z}_\psi^i) - D_{\text{KL}}(q_\psi(\mathbf{z}_i|\mathbf{s}) \parallel p(\mathbf{z}_i))$$

Audio-visual Speech Enhancement

Speech Enhancement



Remove the background noise from the observed mixture speech.

In the short-time Fourier transform (STFT) domain, for all $(f, n) \in \mathbb{B} = \{0, \dots, F - 1\} \times \{0, \dots, N - 1\}$, we observe:

$$x_{fn} = s_{fn} + b_{fn} \quad \text{vectorized representation:} \quad \mathbf{x}_n = \mathbf{s}_n + \mathbf{b}_n$$

- s_{fn} corresponds to **clean speech signal**.
- b_{fn} corresponds to **noise signal**.
- f is the frequency index and n the time-frame index.

Audio-visual Speech Enhancement (AVSE)

- Visual data, i.e. **lips movements**, provides some complementary information about the unknown speech.
- For **highly noisy audio recordings**, visual information can be very helpful.



We aim to efficiently fuse audio and visual modalities for speech enhancement.

Supervised/Unsupervised AVSE

Supervised: Learn a mapping from clean visual data and noisy audio data to clean audio data:

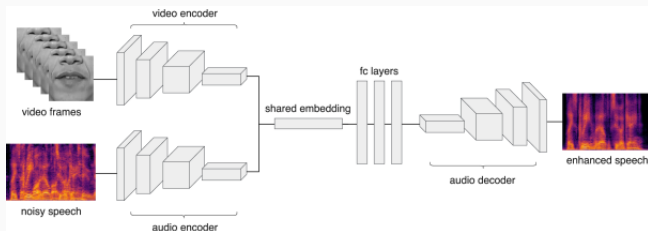


Figure 1: Supervised audio-visual speech enhancement [Gabbby et al., 2018]

Unsupervised (our work): Learn a **generative audio-visual model** for **clean speech** and combine it with an **unsupervised noise model** at test time

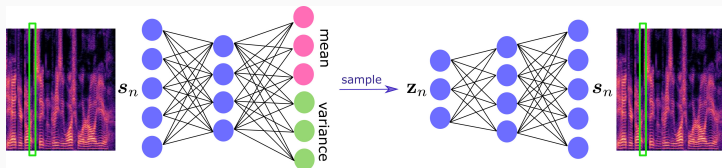
Generative model (Decoder):

Each clean spectrogram time frame s_n is assumed to be generated as:

$$s_n | \mathbf{z}_n \sim \mathcal{N}_c(\mathbf{0}, \text{diag}(\boldsymbol{\sigma}_s(\mathbf{z}_n))), \quad p(\mathbf{z}_n) = \mathcal{N}(\mathbf{0}, \mathbf{I})$$

Inference network (Encoder):

$$q(\mathbf{z}_n | s_n; \psi) = \mathcal{N}(\boldsymbol{\mu}_z^a(s_n), \text{diag}(\boldsymbol{\sigma}_z^a(s_n)))$$



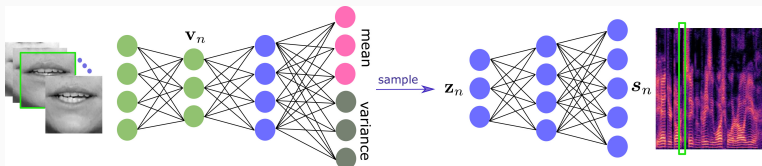
Generative model (Decoder)¹:

$$s_n | \mathbf{z}_n \sim \mathcal{N}_c(\mathbf{0}, \text{diag}(\boldsymbol{\sigma}_s(\mathbf{z}_n))), \quad p(\mathbf{z}_n) = \mathcal{N}(\mathbf{0}, \mathbf{I})$$

Inference network (Encoder):

Infer the posterior using visual data only:

$$q(\mathbf{z}_n | \mathbf{v}_n; \boldsymbol{\psi}) = \mathcal{N}(\boldsymbol{\mu}_z^v(\mathbf{v}_n), \text{diag}(\boldsymbol{\sigma}_z^v(\mathbf{v}_n)))$$



¹M. Sadeghi et al., "Audio-visual Speech Enhancement Using Conditional Variational Auto-Encoder," [Available Online] <https://arxiv.org/abs/1908.02590>, August 2019.

Inspired by conditional VAE (CVAE), use visual data as some deterministic information

Generative network (Decoder):

Each clean spectrogram time frame s_n is assumed to be generated as:

$$\begin{cases} s_n | \mathbf{z}_n, \mathbf{v}_n & \sim \mathcal{N}_c(\mathbf{0}, \text{diag}(\boldsymbol{\sigma}_s(\mathbf{z}_n, \mathbf{v}_n))) \\ \mathbf{z}_n | \mathbf{v}_n & \sim \mathcal{N}(\boldsymbol{\mu}_z(\mathbf{v}_n), \text{diag}(\boldsymbol{\sigma}_z(\mathbf{v}_n))) \end{cases}$$

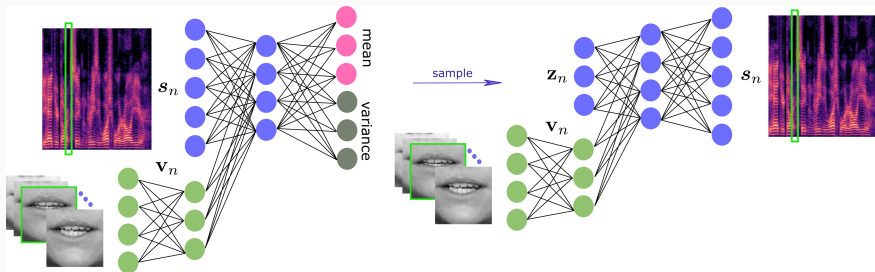
▷ $\mathbf{v}_n$ is an embedding for the image of the speaker lips at frame n .

Inference network (Encoder):

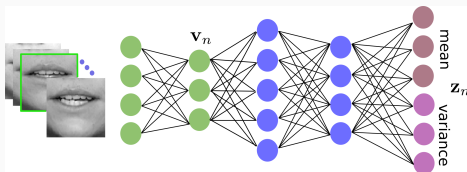
$$q(\mathbf{z}_n | s_n, \mathbf{v}_n; \psi) = \mathcal{N}(\boldsymbol{\mu}_z^{av}(s_n, \mathbf{v}_n), \text{diag}(\boldsymbol{\sigma}_z^{av}(s_n, \mathbf{v}_n)))$$

Audio-visual VAE

Encoder and decoder networks:



Prior distribution for latent variables:



Training samples:

- Clean speech spectrogram time frames: $\{\mathbf{s}_n\}_{n=0}^{N_{tr}-1}$
- Associated visual data: $\{\mathbf{v}_n\}_{n=0}^{N_{tr}-1}$

Optimize the ELBO:

$$\mathcal{L}(\boldsymbol{\theta}, \boldsymbol{\psi}) = \frac{1}{N_{tr}} \sum_{n=0}^{N_{tr}-1} \alpha \cdot \mathbb{E}_{p(\mathbf{z}_n|\mathbf{v}_n)} \left[\ln p(\mathbf{s}_n|\mathbf{z}_n, \mathbf{v}_n; \boldsymbol{\theta}) \right] + \\ (1 - \alpha) \cdot \left(\mathbb{E}_{q(\mathbf{z}_n|\mathbf{s}_n, \mathbf{v}_n; \boldsymbol{\psi})} \left[\ln p(\mathbf{s}_n|\mathbf{z}_n, \mathbf{v}_n; \boldsymbol{\theta}) \right] - D_{\text{KL}} \left(q(\mathbf{z}_n|\mathbf{s}_n, \mathbf{v}_n; \boldsymbol{\psi}) \parallel p(\mathbf{z}_n|\mathbf{v}_n) \right) \right)$$

- $0 \leq \alpha \leq 1$ gives some reconstruction power to the prior network

Speech Enhancement

Noisy speech model: $\forall n : \quad \mathbf{x}_n = \mathbf{s}_n + \mathbf{b}_n$

Noise model: $\forall n : \quad \mathbf{b}_n \sim \mathcal{N}_c(\mathbf{0}, \text{diag}(\mathbf{W}_b \mathbf{H}_b[:, n]))$

Clean speech model: Trained generative network:

$$\begin{cases} p(\mathbf{s}_n | \mathbf{z}_n, \mathbf{v}_n) &= \mathcal{N}_c(\mathbf{0}, \text{diag}(\boldsymbol{\sigma}_s(\mathbf{z}_n, \mathbf{v}_n))) \\ p(\mathbf{z}_n | \mathbf{v}_n) &= \mathcal{N}(\boldsymbol{\mu}_z(\mathbf{v}_n), \text{diag}(\boldsymbol{\sigma}_z(\mathbf{v}_n))) \end{cases}$$

Inference:

- ▷ Parameters to be estimated: $\boldsymbol{\theta}_u = \{\mathbf{W}_b, \mathbf{H}_b\}$
- ▷ Observed variables: $\mathbf{x} = \{\mathbf{x}_n\}_{n=0}^{N-1}, \mathbf{v} = \{\mathbf{v}_n\}_{n=0}^{N-1}$
- ▷ Latent variables: $\mathbf{z} = \{\mathbf{z}_n\}_{n=0}^{N-1}$
- ▷ Likelihood:

$$p(\mathbf{x}_n | \mathbf{z}_n, \mathbf{v}_n; \boldsymbol{\theta}_u) = \mathcal{N}_c(\mathbf{0}, \text{diag}(\boldsymbol{\sigma}_s(\mathbf{z}_n, \mathbf{v}_n)) + \text{diag}(\mathbf{W}_b \mathbf{H}_b[:, n]))$$

Parameter Estimation: MCEM

From an initialization θ_u^* of the parameters, iterate:

- **E-Step:** $Q(\theta_u; \theta_u^*) = \mathbb{E}_{p(\mathbf{z}|\mathbf{x}, \mathbf{v}; \theta_u^*)} [\ln p(\mathbf{x}, \mathbf{z}, \mathbf{v}; \theta_u)].$

Intractable expectation $\rightarrow$ Markov chain Monte Carlo method.

$$Q(\theta_u; \theta_u^*) \approx \frac{1}{R} \sum_{r=1}^R \ln p(\mathbf{x}, \mathbf{z}^{(r)}, \mathbf{v}; \theta_u)$$

The samples $\{\mathbf{z}^{(r)}\}_{r=1, \dots, R}$ are i.i.d. and asymptotically drawn from $p(\mathbf{z}|\mathbf{x}, \mathbf{v}; \theta_u^*)$ using the Metropolis-Hastings method.

▷ Note: $\ln p(\mathbf{x}, \mathbf{z}^{(r)}, \mathbf{v}; \theta_u) = \ln p(\mathbf{x}|\mathbf{z}^{(r)}, \mathbf{v}; \theta_u) + \ln p(\mathbf{z}^{(r)}|\mathbf{v})$

- **M-Step:** $\theta_u^* \leftarrow \operatorname{argmax}_{\theta_u} Q(\theta_u; \theta_u^*).$

Minorize-maximize approach leading to multiplicative update rules.

Speech Estimation

Once the parameters are estimated, the speech STFT frames are estimated via a **Wiener-like filtering** ($\forall f, n$):

$$\begin{aligned}\hat{s}_{fn} &= \mathbb{E}_{p(s_{fn}|x_{fn}, \mathbf{v}_n; \boldsymbol{\theta}_u^*)}[s_{fn}] \\ &= \mathbb{E}_{p(\mathbf{z}_n|\mathbf{x}_n, \mathbf{v}_n; \boldsymbol{\theta}_u^*)} \left[\mathbb{E}_{p(s_{fn}|\mathbf{z}_n, \mathbf{v}_n, \mathbf{x}_n; \boldsymbol{\theta}_u^*)}[s_{fn}] \right] \\ &= \mathbb{E}_{p(\mathbf{z}_n|\mathbf{x}_n, \mathbf{v}_n; \boldsymbol{\theta}_u^*)} \left[\frac{g_n^* \sigma_{s,f}(\mathbf{z}_n, \mathbf{v}_n)}{g_n^* \sigma_{s,f}(\mathbf{z}_n, \mathbf{v}_n) + (\mathbf{W}_b^* \mathbf{H}_b^*)_{f,n}} \right] x_{fn}.\end{aligned}$$

where, $\boldsymbol{\theta}_u^*$ denotes the set of estimated parameters by the MCEM method.

▷ As before, the intractable posterior is approximated by a Markov chain Monte Carlo method.

Experiments

- ▷ **NTCD-TIMIT dataset** [Abdelaziz, 2017]
 - Audio-visual recordings in controlled conditions
 - Clean audio as well as noisy versions
 - Frontal video frames with 30 FPS- 67×67 lips images
- ▷ **Training set** (~ 5 hours): $39 \text{ speakers} \times 98 \text{ sentences} \times 5 \text{ seconds}$
- ▷ **Test set** (~ 1 hour): $9 \text{ speakers} \times 98 \text{ sentences} \times 5 \text{ seconds}$
- ▷ **Noise levels**: -15 dB , -10 dB , -5 dB , 0 dB , 5 dB and 15 dB
- ▷ **Noise types**: *Living Room (LR)*, *White*, *Cafe*, *Car*, *Babble*, and *Street*

Experiments

Networks architectures:

① A-VAE:

- **Decoder:** Single hidden layer, 128 nodes, hyperbolic tangent activations. Input dimension: 32 (latent space).
- **Encoder:** Single hidden layer, 128 nodes, hyperbolic tangent activations. Input dimension: 513 (spectrogram time frame).

② V-VAE:

- **Decoder:** Same as A-VAE.
- **Encoder:** Two hidden layers, 512 and 128 nodes, ReLU activations. Input dimension: 4489 (67×67).

③ AV-VAE: Shares the same architecture as that of AV-VAE with visual embeddings being concatenated with the encoder's and decoder's input.

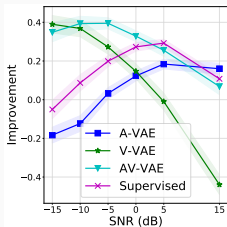
▷ The prior network of the latent variables in AV-VAE takes the same architecture as that of V-VAE's encoder.

Results

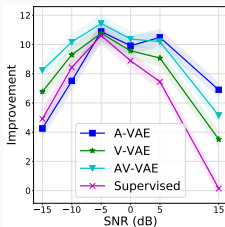
Objective measures (the higher, the better)

- Signal-to-distortion ratio (SDR).
- Perceptual evaluation of speech quality (PESQ) measure.
- Short-time objective intelligibility (STOI).

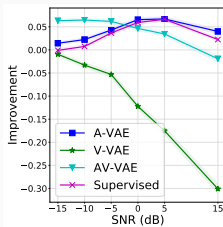
Improvement with respect to the input:



(a) PESQ



(b) SDR



(c) STOI

Audio Examples: <https://team.inria.fr/perception/research/av-vae-se/>

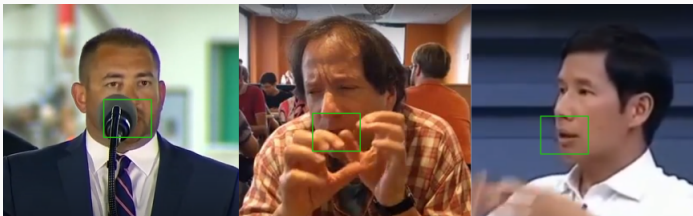
Robust Audio-visual Speech Enhancement

Introduction

AV-VAE usually yields better results than A-VAE, especially at low SNRs, provided **clean (frontal, non-occluded)** visual data [Sadeghi et al., 2019].

Noisy visual data:

Some video frames might contain occluded and/or non-frontal lips region.

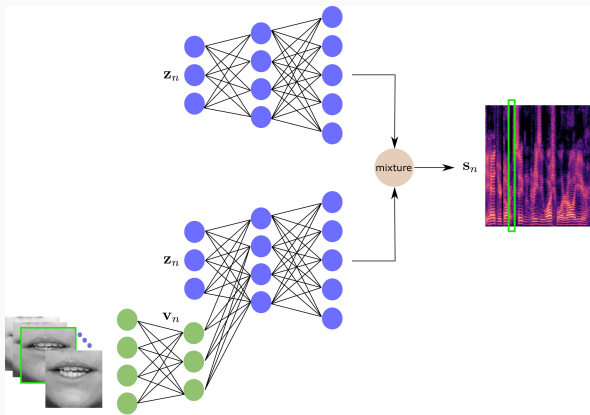


How to effectively benefit from AV-VAE for in-the-wild video recordings?

Our work: VAE mixture model (VAE-MM)

A **mixture** of A-VAE plus AV-VAE generative model:

- If the lips region is clean, use AV-VAE, otherwise use A-VAE.



The A-VAE and AV-VAE have been already trained on clean data.

Generative model

Mixture generative model: Combine A-VAE with AV-VAE

$$\begin{cases} p(\mathbf{s}_n | \mathbf{z}_n, \mathbf{v}_n, \alpha_n) &= \left[\mathcal{N}_c \left(\mathbf{0}, \text{diag}(\boldsymbol{\sigma}_s^a(\mathbf{z}_n)) \right) \right]^{\alpha_n} \times \left[\mathcal{N}_c \left(\mathbf{0}, \text{diag}(\boldsymbol{\sigma}_s^{av}(\mathbf{z}_n, \mathbf{v}_n)) \right) \right]^{1-\alpha_n} \\ p(\mathbf{z}_n | \mathbf{v}_n, \alpha_n) &= \left[\mathcal{N}(\mathbf{0}, \mathbf{I}) \right]^{\alpha_n} \times \left[\mathcal{N} \left(\boldsymbol{\mu}_z^v(\mathbf{v}_n), \text{diag}(\boldsymbol{\sigma}_z^v(\mathbf{v}_n)) \right) \right]^{1-\alpha_n}, \\ p(\alpha_n) &= \pi^{\alpha_n} \times (1 - \pi)^{1-\alpha_n}. \end{cases}$$

$\alpha_n \in \{0, 1\}$ is a latent variable specifying the component of the mixture model that is used by the n -th frame.

Parameter Estimation (test time)

Noisy speech model: $\forall n : \quad \mathbf{x}_n = \mathbf{s}_n + \mathbf{b}_n$

Noise model: $\forall n : \quad \mathbf{b}_n \sim \mathcal{N}_c\left(\mathbf{0}, \text{diag}(\mathbf{W}_b \mathbf{H}_b[:, n])\right)$

Clean speech model: Mixture of A-VAE and AV-VAE generative networks

Inference:

- ▷ Observed variables: $\{\mathbf{x}_n, \mathbf{v}_n\}_{n=0}^{N-1}$
- ▷ Latent variables: $\{\mathbf{s}_n, \mathbf{z}_n, \alpha_n\}_{n=0}^{N-1}$
- ▷ Parameters to be estimated: $\boldsymbol{\theta}_u = \{\mathbf{W}_b, \mathbf{H}_b, \pi\}$

Parameter Estimation (test time)

Variational Expectation-maximization (VEM)

Variational E-Step:

The intractable posterior $p(\mathbf{s}_n, \mathbf{z}_n, \alpha_n | \mathbf{x}_n, \mathbf{v}_n; \boldsymbol{\theta}_u)$ is approximated by a variational distribution factorizing as follows:

$$r(\mathbf{s}_n, \mathbf{z}_n, \alpha_n) = r(\mathbf{s}_n) r(\mathbf{z}_n) r(\alpha_n).$$

The update formulas for the variational distributions [Bishop, 2006]:

VE $\mathbf{s}_n$ -step: $r(\mathbf{s}_n) \propto \exp \left(\mathbb{E}_{r(\mathbf{z}_n) \cdot r(\alpha_n)} \left[\log p(\mathbf{x}_n, \mathbf{s}_n, \mathbf{z}_n, \alpha_n, \mathbf{v}_n; \boldsymbol{\theta}_u) \right] \right)$

VE $\mathbf{z}_n$ -step: $r(\mathbf{z}_n) \propto \exp \left(\mathbb{E}_{r(\mathbf{s}_n) \cdot r(\alpha_n)} \left[\log p(\mathbf{x}_n, \mathbf{s}_n, \mathbf{z}_n, \alpha_n, \mathbf{v}_n; \boldsymbol{\theta}_u) \right] \right)$

VE α_n -step: $r(\alpha_n) \propto \exp \left(\mathbb{E}_{r(\mathbf{s}_n) \cdot r(\mathbf{z}_n)} \left[\log p(\mathbf{x}_n, \mathbf{s}_n, \mathbf{z}_n, \alpha_n, \mathbf{v}_n; \boldsymbol{\theta}_u) \right] \right)$

$$r(\mathbf{s}_n) = \mathcal{N}_c(\mathbf{m}_n, \text{diag}(\boldsymbol{\nu}_n)), \quad \begin{cases} m_{fn} &= \frac{\gamma_{fn}}{\gamma_{fn} + (\mathbf{W}_b \mathbf{H}_b)_{fn}} \cdot x_{fn} \\ \nu_{fn} &= \frac{\gamma_{fn} \cdot (\mathbf{W}_b \mathbf{H}_b)_{fn}}{\gamma_{fn} + (\mathbf{W}_b \mathbf{H}_b)_{fn}} \end{cases}$$

which can be interpreted is an **averaged Wiener filtering**.

$$\gamma_{fn}^{-1} = \sum_{\alpha_n \in \{0,1\}} r(\alpha_n) \cdot \eta_{fn}^{\alpha_n} \quad (\text{weighted precision over audio and audio-visual cases}),$$

$$\eta_{fn}^{\alpha_n} = \mathbb{E}_{r(\mathbf{z}_n)} \left[\frac{1}{\sigma_{s,f}^{\alpha_n}(\mathbf{z}_n, \mathbf{v}_n)} \right] \approx \frac{1}{D} \sum_{d=1}^D \frac{1}{\sigma_{s,f}^{\alpha_n}(\mathbf{z}_n^{(d)}, \mathbf{v}_n)} \quad (\text{average precision}),$$

and $\{\mathbf{z}_n^{(d)}\}_{d=1}^D$ is a sequence sampled from $r(\mathbf{z}_n)$. Moreover:

$$\sigma_{s,f}^{\alpha_n}(\mathbf{z}_n, \mathbf{v}_n) = \begin{cases} \sigma_{s,f}^a(\mathbf{z}_n) & \alpha_n = 1 \\ \sigma_{s,f}^{av}(\mathbf{z}_n, \mathbf{v}_n) & \alpha_n = 0 \end{cases}.$$

For $r(\mathbf{z}_n)$ we obtain the following result:

$$r(\mathbf{z}_n) \propto \exp \left(\sum_{\alpha_n \in \{0,1\}} r(\alpha_n) \cdot \left[\log p(\mathbf{z}_n | \mathbf{v}_n, \alpha_n) + \sum_f -\log \left(\sigma_{s,f}^{\alpha_n}(\mathbf{z}_n, \mathbf{v}_n) \right) - \frac{|m_{fn}|^2 + \nu_{fn}}{\sigma_{s,f}^{\alpha_n}(\mathbf{z}_n, \mathbf{v}_n)} \right] \right).$$

The above distribution cannot be computed in closed-form. Nevertheless, we can draw samples from it using the **Metropolis-Hastings** (MH) algorithm (see our paper for more details).

To update the variational distribution of α_n , we can write:

$$r(\alpha_n) \propto \exp \left(\mathbb{E}_{r(\mathbf{s}_n) \cdot r(\mathbf{z}_n)} \left[\log p(\mathbf{s}_n | \mathbf{z}_n, \mathbf{v}_n, \alpha_n) + \log p(\mathbf{z}_n | \mathbf{v}_n, \alpha_n) + \log p(\alpha_n) \right] \right)$$

which is a Bernoulli distribution with

$$\pi_n = g \left(\mathbb{E}_{r(\mathbf{s}_n) \cdot r(\mathbf{z}_n)} \left[\log \frac{p(\mathbf{s}_n, \mathbf{z}_n | \mathbf{v}_n, \alpha_n = 1)}{p(\mathbf{s}_n, \mathbf{z}_n | \mathbf{v}_n, \alpha_n = 0)} \right] + \log \frac{\pi}{1 - \pi} \right)$$

as the parameter, which is an **averaged audio/audio-visual ratio**. Here, $g(\cdot)$ denotes the sigmoid function defined as $g(x) = 1/(1 + \exp(-x))$.

Parameters Update and Speech Estimation

M-Step:

Update parameters by optimizing the complete data log-likelihood:

$$\begin{aligned} Q(\boldsymbol{\theta}_u, \boldsymbol{\theta}_u^{\text{old}}) &\stackrel{c}{=} \mathbb{E}_{r(\mathbf{s}_n) \cdot r(\mathbf{z}_n) \cdot r(\alpha_n)} \left[\log p(\mathbf{x}_n, \mathbf{s}_n, \mathbf{z}_n, \alpha_n, \mathbf{v}_n; \boldsymbol{\theta}_u) \right] \\ &\stackrel{c}{=} \sum_{f,n} -\log (\mathbf{W}_b \mathbf{H}_b)_{fn} - \left(\frac{|x_{fn} - m_{fn}|^2 + \nu_{fn}}{(\mathbf{W}_b \mathbf{H}_b)_{fn}} \right) \\ &\quad + \pi_n \log \pi + (1 - \pi_n) \log(1 - \pi). \end{aligned}$$

Speech Estimation:

After the convergence of the VEM, the speech STFT frames are estimated using an **averaged Wiener filtering**:

$$\hat{s}_{fn} = \mathbb{E}_{r(s_{fn})}[s_{fn}] = \frac{\gamma_{fn}^*}{\gamma_{fn}^* + (\mathbf{W}_b^* \mathbf{H}_b^*)_{fn}} \cdot x_{fn} \quad \forall (f, n)$$

Experiments

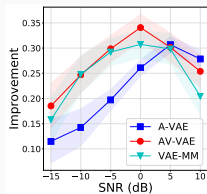
- **Noisy+clean speech:** NTCD-TIMIT database [Abdelaziz, 2017]
- **VAE models:** Pre-trained A-VAE and AV-VAE [Sadeghi et al., 2019]
- **Setup:**
 - Testing set of NTCD-TIMIT database;
 - ~ 1 hours of speech;
 - 9 speakers;
 - Noise types: *LR*, *White*, *Cafe*, *Car*, *Babble*, and *Street*;
 - Noise levels: $-15, -10, -5, 0, 5, 10$ dB;
 - 270 noisy mixtures per noise level;
 - **Different speakers and sentences** than in the training set;
 - Clean lips region as well as noisy versions ($\sim$ one-third of total video frames per sample)

Results

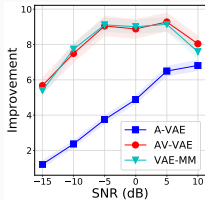
Objective measures (the higher, the better)

- Signal-to-distortion ratio (SDR).
- Perceptual evaluation of speech quality (PESQ) measure.

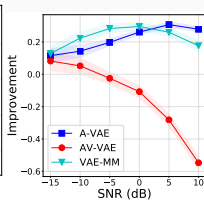
Improvement with respect to the input:



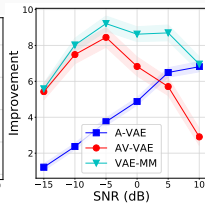
(a) PESQ(clean)



(b) SDR(clean)



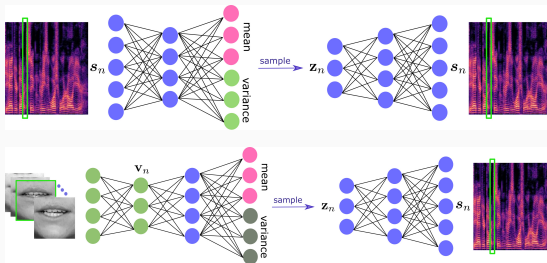
(c) PESQ(noisy)



(d) SDR(noisy)

Mixture of Audio-visual Inference Networks

Introduction

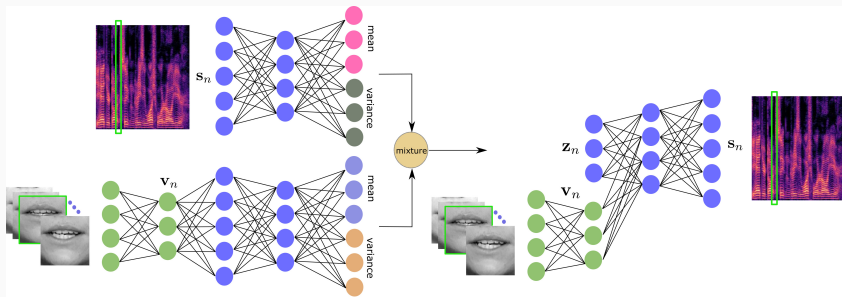


- ▷ **Initialization of latent codes at test phase:** Posterior mean of the encoder.
A-VAE: inputs **noisy** speech, while V-VAE inputs **clean** visual data.
- ▷ **Better audio-visual fusion:** Concatenating audio and visual data or tight fusion (AV-VAE) is not good when one modality is very weak.

How to take advantage of both A-VAE and V-VAE and provide a better audio-visual fusion?

Mixture of Inference Networks VAE (MIN-VAE)

Train a mixture of audio and visual inference networks:²



- 👉 The shared generative model (decoder) is trained using both audio and visual latent codes
- 👉 Once trained, the latent codes at test phase can be initialized using the visual encoder

²M. Sadeghi and X. Alameda-Pineda, "Mixture of Inference Networks for VAE-based Audio-visual Speech Enhancement,"

Mixture of Inference Networks: Generative Model

The generative model for each s_n :

$$\begin{aligned} s_n | \mathbf{z}_n, \mathbf{v}_n &\sim \mathcal{N}(\mathbf{0}, \text{diag}(\boldsymbol{\sigma}_s(\mathbf{z}_n, \mathbf{v}_n))) \\ \mathbf{z}_n | \alpha_n &\sim \left[\mathcal{N}(\boldsymbol{\mu}_a, \sigma_a \mathbf{I}) \right]^{\alpha_n} \cdot \left[\mathcal{N}(\boldsymbol{\mu}_v, \sigma_v \mathbf{I}) \right]^{1-\alpha_n} \\ \alpha_n &\sim \pi^{\alpha_n} \times (1 - \pi)^{1-\alpha_n} \end{aligned}$$

- Each latent code, $\mathbf{z}_n$, is generated either from an **audio** or from a **video** prior,
- The audio and video priors are parametrized by $(\boldsymbol{\mu}_a, \sigma_a)$ and $(\boldsymbol{\mu}_v, \sigma_v)$,
- A mixing variable $\alpha_n \in \{0, 1\}$ describes whether $\mathbf{z}_n$ corresponds to the **audio** or to the **video** prior.

Training MIN-VAE

Posterior distribution of the latent variables:

$$p(\mathbf{z}_n, \alpha_n | \mathbf{s}_n, \mathbf{v}_n) = p(\mathbf{z}_n | \mathbf{s}_n, \mathbf{v}_n, \alpha_n) \cdot p(\alpha_n | \mathbf{s}_n, \mathbf{v}_n).$$

The two posteriors in the RHS are intractable. We assume some variational approximation:

$$q(\mathbf{z}_n | \mathbf{s}_n, \mathbf{v}_n, \alpha_n; \phi) = \begin{cases} q(\mathbf{z}_n | \mathbf{s}_n; \phi_a) & \alpha_n = 1 \text{ (audio encoder)} \\ q(\mathbf{z}_n | \mathbf{v}_n; \phi_v) & \alpha_n = 0 \text{ (video encoder)} \end{cases}$$

A variational distribution, denoted $r(\alpha_n)$, is considered for $p(\alpha_n | \mathbf{s}_n, \mathbf{v}_n)$.

Final approximation

$$p(\mathbf{z}_n, \alpha_n | \mathbf{s}_n, \mathbf{v}_n) \approx q(\mathbf{z}_n | \mathbf{s}_n, \mathbf{v}_n, \alpha_n; \phi) \cdot r(\alpha_n)$$

Inference:

- ▷ Observed variables: $\mathbf{s} = \{\mathbf{s}_n\}_{n=0}^{N_{tr}-1}$ and $\mathbf{v} = \{\mathbf{v}_n\}_{n=0}^{N_{tr}-1}$
 - ▷ Latent variables: $\mathbf{z} = \{\mathbf{z}_n\}_{n=0}^{N_{tr}-1}$ and $\boldsymbol{\alpha} = \{\alpha_n\}_{n=0}^{N_{tr}-1}$
 - ▷ Parameters to be estimated: $\boldsymbol{\Theta} = \{\psi, \phi, \pi, \boldsymbol{\mu}_a, \boldsymbol{\mu}_v, \sigma_a, \sigma_v\}$ and r
-

We target a lower bound on the data log-likelihood $\log p(\mathbf{s}, \mathbf{v}; \boldsymbol{\theta})$:

$$\begin{aligned} \max_{\boldsymbol{\Theta}, r} \mathcal{L}(\boldsymbol{\Theta}, r) = \\ \max_{\boldsymbol{\Theta}, r} \int_{\mathbb{Z}, \mathbb{A}} q(\mathbf{z}|\mathbf{s}, \mathbf{v}, \boldsymbol{\alpha}; \boldsymbol{\psi}) r(\boldsymbol{\alpha}) \log \frac{p(\mathbf{s}|\mathbf{z}; \boldsymbol{\theta}) p(\mathbf{z}|\boldsymbol{\alpha}) p(\boldsymbol{\alpha})}{q(\mathbf{z}|\mathbf{s}, \mathbf{v}, \boldsymbol{\alpha}; \boldsymbol{\psi}) r(\boldsymbol{\alpha})} d\mathbf{z} d\boldsymbol{\alpha} \end{aligned}$$

Training MIN-VAE

- $r(\alpha_n) = \pi_n^{\alpha_n} \cdot (1 - \pi_n)^{1-\alpha_n}$

$$\begin{cases} \pi_n = g\left(J_n(\alpha_n = 0) - J_n(\alpha_n = 1) + \log \frac{\pi}{1-\pi}\right), \\ J_n(\alpha_n) = \mathcal{D}_{KL}\left(q(\mathbf{z}_n|\mathbf{s}_n, \mathbf{v}_n, \alpha_n; \phi) \parallel p(\mathbf{z}_n|\alpha_n)\right) - \log p(\mathbf{s}_n|\mathbf{z}_n^{\alpha_n}, \mathbf{v}_n; \theta) \\ \mathbf{z}_n^{\alpha_n} \sim q(\mathbf{z}_n|\mathbf{s}_n, \mathbf{v}_n, \alpha_n; \phi) \end{cases}$$

- Θ is updated by:

$$\min_{\Theta} \sum_{n=0}^{N_{tr}} \mathbb{E}_{r(\alpha_n)} \left[J_n(\alpha_n) \right] + \mathcal{D}_{KL}\left(r(\alpha_n) \parallel p(\alpha_n)\right)$$

- Stochastic gradient descent for $\phi, \theta, \mu_a, \mu_v, \sigma_a, \sigma_v$
- $\pi = \frac{1}{N_{tr}} \sum_{n=1}^{N_{tr}} \pi_n$

Parameter Estimation (test time)

Noisy speech model: $\forall n : \mathbf{x}_n = \mathbf{s}_n + \mathbf{b}_n$

Noise model: $\forall n : \mathbf{b}_n \sim \mathcal{N}_c(\mathbf{0}, \text{diag}(\mathbf{W}_b \mathbf{H}_b[:, n]))$

Clean speech model: Trained MIN-VAE

$$\begin{aligned} \mathbf{s}_n | \mathbf{z}_n, \mathbf{v}_n &\sim \mathcal{N}(\mathbf{0}, \text{diag}(\boldsymbol{\sigma}_s(\mathbf{z}_n, \mathbf{v}_n))) \\ \mathbf{z}_n | \alpha_n &\sim \left[\mathcal{N}(\boldsymbol{\mu}_a, \sigma_a \mathbf{I}) \right]^{\alpha_n} \cdot \left[\mathcal{N}(\boldsymbol{\mu}_v, \sigma_v \mathbf{I}) \right]^{1-\alpha_n} \\ \alpha_n &\sim \pi^{\alpha_n} \times (1 - \pi)^{1-\alpha_n} \end{aligned}$$

Inference:

- ▷ Observed variables: $\{\mathbf{x}_n, \mathbf{v}_n\}_{n=0}^{N-1}$
- ▷ Latent variables: $\{\mathbf{s}_n, \mathbf{z}_n, \alpha_n\}_{n=0}^{N-1}$
- ▷ Parameters to be estimated: $\boldsymbol{\theta}_u = \{\mathbf{W}_b, \mathbf{H}_b, \pi\}$

Parameter Estimation (test time)

Intractable posterior $\rightarrow$ variational approximation:

$$r(\mathbf{s}_n, \mathbf{z}_n, \alpha_n) = r(\mathbf{s}_n) \times r(\mathbf{z}_n) \times r(\alpha_n)$$

VE $\mathbf{s}_n$ -step: $r(\mathbf{s}_n) = \mathcal{N}_c(m_{fn}, \nu_{fn}), \begin{cases} m_{fn} &= \frac{\gamma_{fn}}{\gamma_{fn} + (\mathbf{W}\mathbf{H})_{fn}} \cdot x_{fn} \\ \nu_{fn} &= \frac{\gamma_{fn} \cdot (\mathbf{W}\mathbf{H})_{fn}}{\gamma_{fn} + (\mathbf{W}\mathbf{H})_{fn}} \\ \gamma_{fn}^{-1} &= \frac{1}{D} \sum_{d=1}^D \frac{1}{\sigma_{s,f}(\mathbf{z}_n^{(d)}, \mathbf{v}_n)} \\ \mathbf{z}_n^{(d)} &\sim r(\mathbf{z}_n), \quad d = 1, \dots, D \end{cases}$

VE $\mathbf{z}_n$ -step:
$$r(\mathbf{z}_n) \propto \exp \left(\sum_f -\log \left(\sigma_{s,f}(\mathbf{z}_n, \mathbf{v}_n) \right) - \frac{|m_{fn}|^2 + \nu_{fn}}{\sigma_{s,f}(\mathbf{z}_n, \mathbf{v}_n)} \right. \\ \left. + \sum_{\alpha_n \in \{0,1\}} r(\alpha_n) \cdot \left[\log p(\mathbf{z}_n | \alpha_n) \right] \right)$$

VE α_n -step:
$$r(\alpha_n) = \pi_n^{\alpha_n} \cdot (1 - \pi_n)^{1 - \alpha_n},$$

$$\pi_n = g \left(\mathbb{E}_{r(\mathbf{z}_n)} \left[\log \frac{p(\mathbf{z}_n | \alpha_n = 1)}{p(\mathbf{z}_n | \alpha_n = 0)} \right] + \log \frac{\pi}{1 - \pi} \right)$$

Parameters Update and Speech Estimation

M-Step:

Update parameters by optimizing the complete data log-likelihood:

$$\begin{aligned} Q(\boldsymbol{\theta}_u, \boldsymbol{\theta}_u^{\text{old}}) &\stackrel{c}{=} \mathbb{E}_{r(\mathbf{s}_n) \cdot r(\mathbf{z}_n) \cdot r(\alpha_n)} \left[\log p(\mathbf{x}_n, \mathbf{s}_n, \mathbf{z}_n, \alpha_n, \mathbf{v}_n; \boldsymbol{\theta}_u) \right] \\ &\stackrel{c}{=} \mathbb{E}_{r(\mathbf{s}_n)} \left[\log p(\mathbf{x}_n | \mathbf{s}_n; \boldsymbol{\theta}_u) \right] + \mathbb{E}_{r(\alpha_n)} \left[\log p(\alpha_n) \right] \\ &\stackrel{c}{=} \sum_{f,n} -\log (\mathbf{W}_b \mathbf{H}_b)_{fn} - \left(\frac{|x_{fn} - m_{fn}|^2 + \nu_{fn}}{(\mathbf{W}_b \mathbf{H}_b)_{fn}} \right) \\ &\quad + \pi_n \log \pi + (1 - \pi_n) \log(1 - \pi). \end{aligned}$$

Speech Estimation:

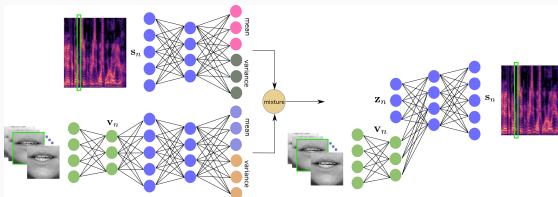
After the convergence of the VEM, the speech STFT frames are estimated using an **averaged Wiener filtering**:

$$\hat{s}_{fn} = \mathbb{E}_{r(s_{fn})}[s_{fn}] = \frac{\gamma_{fn}^*}{\gamma_{fn}^* + (\mathbf{W}_b^* \mathbf{H}_b^*)_{fn}} \cdot x_{fn} \quad \forall(f, n)$$

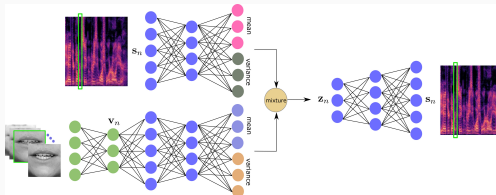
Experiments

Settings similar as before with the NTCD-TIMIT dataset

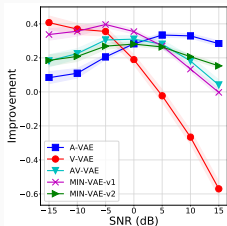
MIN-VAE-v1:



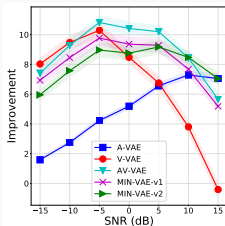
MIN-VAE-v2:



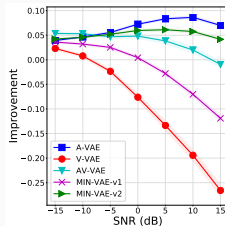
Results



(a) PESQ

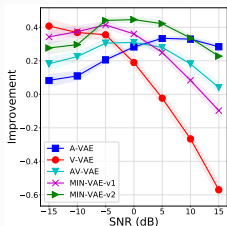


(b) SDR

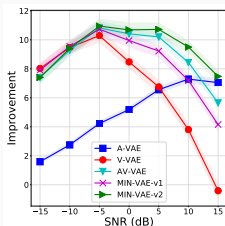


(c) STOI

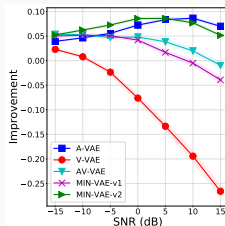
Adding noise to one-third of spectrograms input to audio-encoder:



(d) PESQ



(e) SDR



(f) STOI

Conclusion and Future Work

Variational autoencoders provide efficient ways to fuse audio and visual modalities for clean speech modeling and speech enhancement.

- The VEM framework is slow. Trying to re-use the trained encoders at inference time can reduce the complexity.
- Temporal modeling of the latent variables to benefit from time dependency between audio as well as visual frames.
- Extending the robust VAE to more than two models: A-VAE, V-VAE, and AV-VAE.

Thank you for your attention

References

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